## Applied Optimization

## Goal

We will learn how to solve applied optimization (maximum and minimum) problems. There are 2 categories of problems:

1. Problems that deal with maximizing or minimizing a continuous function over a finite closed interval.
2. Problems that deal with maximizing or minimizing a continuous function over an infinite interval or a finite interval that is not closed.

In either case, we need to consider the feasible domain of the problem and then use techniques that we have already learned to maximize or minimize a particular function. Part of finding the solution to a given problem is making sure that we have actually found a solution.

## Guidelines for Solving Applied Optimization Problems

1. Identify all given quantities and quantities to be determined. If possible, draw a picture.
2. Write a primary equation for the quantity that is to be maximized or minimized.
3. Reduce the primary equation to one having a single independent variable. This may involve the use of a secondary equation relating the independent variables of the primary equation.
4. Determine the feasible domain of the primary equation (this is some subset of the natural domain). That is, determine the values for which the stated problem makes sense.
5. Determine desired max or min value by using the techniques of the previous sections.

Important Note 1. Sometimes we want to know what the max or min is and sometimes we want to know when the max or min occurs.

## Examples

Let's do a few examples.
Example 2. Find two positive numbers such that their product is 192 and the sum of the first and three times the second is as small as possible.

Example 3. A farmer has 500 feet of fencing with which to enclose a pasture for grazing nuggets. The farmer only need to enclose 3 sides of the pasture since the remaining side is bounded by a river (no, nuggets can't swim). In addition, some of the nuggets don't get along with some of the other nuggets. He plans to separate the troublesome nuggets by forming 2 adjacent corrals. Determine the dimensions that would yield the maximum area for the pasture.

Example 4. An open box is to be made from a 16 -inch by 30 -inch piece of cardboard by cutting out squares of equal size from each of the four corners and bending up the sides. What size should the squares be to obtain a box with the largest volume?

Example 5. An interstellar nugget travels along a path given by $p(x)=4-x^{2}$. If a star is located at the point $(0,2)$, find the point(s) on the path of the nugget that are closest to the star.

