

## Exam 1 (Part 2)

Your Name:

Names of Any Collaborators:

### Instructions

Answer each of the following questions and then submit your solutions to BbLearn by **11:59pm on Friday, February 26**. You can either write your solutions on paper and then capture your work digitally or you can write your solutions digitally on a tablet (e.g., iPad). This part of Exam 1 is worth a total of 12 points and is worth 30% of your overall score on Exam 1. Your overall score on Exam 1 is worth 20% of your overall grade.

I expect your solutions to be *well-written, neat, and organized*. Do not turn in rough drafts. What you turn in should be the “polished” version of potentially several drafts. Feel free to type up your final version. The  $\text{\LaTeX}$  source file of this exam is also available if you are interested in typing up your solutions using  $\text{\LaTeX}$ . I’ll gladly help you do this if you’d like.

Reviewing material from previous courses and looking up definitions and theorems you may have forgotten is fair game. However, when it comes to completing the following problems, you should *not* look to resources outside the context of this course for help. That is, you should not be consulting the web, other texts, other faculty, or students outside of our course in an attempt to find solutions to the problems you are assigned. This includes Chegg and Course Hero. On the other hand, you may use each other, the textbook, me, and your own intuition. Further information:

1. You may freely use any theorems that we have discussed in class, but you should make it clear where you are using a previous result and which result you are using. For example, if a sentence in your proof follows from Problem 3.16, then you should say so.
2. Unless you prove them, you cannot use any results from the course notes that we have not yet covered.
3. You are **NOT** allowed to consult external sources when working on the exam. This includes people outside of the class, other textbooks, and online resources.
4. You are **NOT** allowed to copy someone else’s work.
5. You are **NOT** allowed to let someone else copy your work.
6. You are allowed to discuss the problems with each other and critique each other’s work.

**I will vigorously pursue anyone suspected of breaking these rules.**

You should **turn in this cover page** and all of the work that you have decided to submit. **Please write your solutions and proofs on your own paper.** To convince me that you have read and understand the instructions, sign in the box below.

Signature:

Good luck and have fun!

For some of these problems you will need to digest some new content in the book. We will spend some time discussing these concepts in class during the time you have available to work on the exam.

1. (4 points) Complete **one** of the following.

(a) Problem 3.29.

(b) Prove that if  $(p_i)_{i=1}^{\infty}$  is a sequence that converges to  $x \neq 0$  such that  $p_i \neq 0$  for all  $i$ , then the sequence determined by  $q_i = \frac{1}{p_i}$  converges to  $\frac{1}{x}$ .

(c) Prove that if  $M$  is a set with accumulation point  $x$ , then there exists a sequence  $(m_i)_{i=1}^{\infty}$  that converges to  $x$  such that each  $m_i \in M$  and either  $m_i < m_{i+1}$  for all  $i$  (i.e., sequence is increasing) or  $m_i > m_{i+1}$  for all  $i$  (i.e., sequence is decreasing).

2. (4 points) Complete **one** of the following.

(a) Problem 3.35(a).

(b) Problem 3.35(b).

3. (4 points) Complete Problem 3.43.