

Problem 3.61

$$(C) \quad A \times (B \cap C) = (A \times B) \cap (A \times C)$$

Pf: let A, B, C be sets.

(\subseteq) let $(x, y) \in A \times (B \cap C)$. By def of Cartesian product, $x \in A$ and $y \in B \cap C$.

By def of int, $y \in B$ and $y \in C$. By

def Cart prod, $(x, y) \in A \times B$ and

$(x, y) \in A \times C$. So, $(x, y) \in (A \times B) \cap (A \times C)$.

(\supseteq) Reverse above.